## Vulnerability analysis of Salsa20

Differential analysis and deep learning analysis of Salsa20.

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This thesis is worth 30 study points

## Summary

This work attempts to address the research question of how secure the current solutions in lightweight cryptography are, and specifically, if Salsa20 is a sufficiently secure algorithm for its intended purposes.

We perform a state of the art survey on the current landscape of lightweight cryptography and a survey of the cryptanalysis most relevant to these kinds of crypto systems. We take a closer look at the ARX-based stream cipher Salsa20, analyse its security and give recommendation based on the results.

We implement two analyses against both Salsa20 and one of its code components, the quarter-round function. While breaking the quarter-round may not be useful for breaking Salsa20, it gives us an idea of the viability of the analysis. The two analysis methods are:

1. Differential analysis using the Hamming distance.

We found that the quarter-round, when treated like an encryption algorithm, had an insufficient avalanche effect and is easily distinguishable from random noise for chosen plaintexts. We could not find any indication the full Salsa20 algorithm suffer from these effects.
2. Deep learning-based analysis using a context aggregation network. This analysis used images (some generated from random noise, some actual images), encrypted them, and tested if the context aggregation network (CAN) was able to learn and reconstruct parts of the original images or plaintexts. The results indicated this method is not viable against either Salsa20 nor its quarter-round function.

We therefore conclude that these forms of analysis does not seem effective against Salsa20.

## Acknowledgments

This master thesis was written at the University of South-Eastern Norway, with the assistance of two supervisors:

1. Professor Daniel Larsson, University of South-Eastern Norway (USN), Faculty of Technology, Natural Sciences and Maritime Sciences, Kongsberg.
2. Associate Professor Kiran Raja, Norwegian University of Science and Technology (NTNU), Faculty of Information Technology and Electrical Engineering, Gjøvik.

I would like to thank my two supervisors. Their help and support have been vital to the work. Thanks to Julie for keeping me sane during the COVID-19 lockdown. Thanks to friends and family, and especially from my mother, for their support.

## Contents

1 Introduction ..... 9
2 Background ..... 12
2.1 IoT and mesh network security ..... 12
2.2 Basics of cryptography ..... 14
2.2.1 Encryption algorithms ..... 14
2.2.2 Hashing algorithms ..... 19
2.3 Lightweight cryptography ..... 21
2.4 State of the art - Lightweight cryptography ..... 22
2.5 Cryptanalysis ..... 29
2.6 Cryptanalysis of Salsa20 ..... 32
2.7 Context aggregation networks ..... 32
3 Methodology ..... 35
3.1 Detailed description of Salsa20 ..... 35
3.1.1 ARX ..... 35
3.1.2 Overview of Salsa20 ..... 36
3.2 How ChaCha differs from Salsa20 ..... 42
3.3 Analysis on Salsa20 ..... 43
3.3.1 Test setup ..... 44
3.3.2 Brute-force estimation ..... 44
3.3.3 Hamming distance differential analysis ..... 45
3.3.4 CAN analysis ..... 47
4 Results and discussion ..... 53
4.1 Hamming distance ..... 53
4.1.1 Quarter-round function ..... 53
4.1.2 Salsa20's PRG ..... 55
4.2 Context aggregation network ..... 56
5 Conclusion ..... 60
5.1 Further work ..... 60

## List of Figures

2.1 Structure of a traditional star-formed network. ..... 13
2.2 Example of structure of a mesh network ..... 13
2.3 Design trade-offs in lightweight cryptography. ..... 22
3.1 Overview of the structure of Salsa20. ..... 37
3.2 Flowchart of the Salsa20 quarter-round function. ..... 41
3.3 Flowchart of the ChaCha quarter-round function. ..... 43
3.4 Algorithm for the differential HD analysis on $X-Y$ pairs. ..... 46
3.5 Algorithm for CAN analysis on PT-CT pairs. ..... 47
3.6 Example of an incremented PT-CT pair ..... 49
3.7 Example of a random PT-CT pair. ..... 49
3.8 Example of a randomly generated PT-CT pair converted into RGB images ..... 49
3.9 Example of a randomly generated plaintext converted into an black and white image ..... 50
3.10 Illustration of our plaintext-based CAN analysis method ..... 50
3.11 Algorithm for CAN analysis on PT-CT pairs. ..... 51
3.12 Image version of the CT from an encrypted image of a face ..... 51
3.13 Illustration of our image-based CAN analysis. ..... 52
4.1 Effects of flipping random bits in $X$ ..... 54
4.2 Averaging of effects on $Y$ when bits are flipped in $X$ ..... 55
4.3 Averaging of effects on the PRG output when bits are flipped in key ..... 56
4.4 Training trend for regular images ..... 57
4.5 Training trend for the QR text pairs. ..... 57
4.6 Training trend for the Salsa20 text pairs. ..... 58
4.7 Training trend for the Salsa20 image pairs, with patch size of $256 \times 256$. ..... 59
4.8 Training trend for the Salsa20 image pairs, with patch size of $32 \times 32$. ..... 59

## List of Tables

1 List of abbreviations, with short descriptions. ..... 8
2.1 Types of cipher structures ..... 17
2.2 eSTREAM portfolio. ..... 23
2.3 Explanation of terms used in the state of the art analysis. ..... 24
2.4 Technical information of block ciphers. ..... 25
2.5 Technical information of stream ciphers. ..... 25
2.6 Technical information of hash functions. ..... 25
2.7 Pros and cons of block ciphers ..... 26
2.8 Pros and cons of stream ciphers. ..... 27
2.9 Pros and cons of hashing algorithms. ..... 28
2.10 Amount of knowledge the attacker has access to. ..... 29
2.11 Cryptanalysis techniques and attacks for symmetric ciphers. ..... 31
2.12 Potential attacks against Salsa20. ..... 33
2.13 Some existing protection methods against cryptographic attacks. ..... 34
3.1 Salsa20's initialization vectors (IVs) ..... 38
3.2 Salsa20's initial state (IS) for 32 byte keys. ..... 38
3.3 The 16 binary words being used in the double-round function. ..... 41
3.4 Results from the speed performance test. ..... 44
3.5 Plaintext-ciphertext pairs generated for CAN analysis. ..... 48

| Abbr | Phrase | Short description |
| :---: | :---: | :---: |
| ARX | Modular Addition, <br> Rotation and XOR | A type of cipher structure. |
| CAN | Context, <br> Aggregation and Network | A machine learning/deep learning technique, which is used to generate or modify images, based on learned behaviour. |
| ECC | Elliptic Curve <br> Cyptography | A category of asymmetric cryptographic algorithms. |
| GE | Gate Equivalent | Estimate on how many logical gates on a processing unit an algorithm implementation requires. |
| HD | Hamming Distance | Amount of bit-by-bit differences between two binary numbers. |
| HW | Hamming Weight | Amount of non-zero bits in a binary number. |
| HW | Hardware | Physical implementation or systems. (As opposed to virtual software systems.) |
| IS | Internal State | The internal temporary values in a cryptographic systems. |
| IV | Initialization Vector | A set of initial starting values of a cryptographic system. These are generally static values. |
| PRG | Pseudo Random number Generator | A function or system which generates pseudorandom values, based on some seed value(s). |
| PRP | Psudo Random <br> Permutation | Similar to a PRG, but makes a pseudorandom one-to-one mapping. |
| PT/CT | Plaintext / <br> Claintext | The input text, message, file or general data of an encryption algorithm (PT), and its encrypted version (CT). |
| QR | Quarter-Round function | The core function of the Salsa family encryption algorithms. |
| SPN | Substitution- <br> Permutation Network | A type of cipher structure. |
| SW | Software | Virtual implementations or systems. (As opposed to physical hardware systems.) |
| XOR | Exclusive or | A function which does a bit-by-bit comparison between two binary numbers. |

Table 1: List of abbreviations, with short descriptions.

## Chapter 1

## Introduction

As microprocessors become cheaper, the Internet of Things (IoT) become more prevalent. Because to this, we see this kind of technology take a bigger and bigger part of our lives. However, this brings up questions of computer security and privacy. We expect our data to be protected from unwanted listeners and hackers who want to steal it, modify it or destroy it. We also expect the newest technology available at low cost. As the technology for IoT is strongly connected to networks and the internet, its capability to affect our lives in negative ways grows. It is therefore important to protect our data and our devices from unwanted attackers. Cryptography is the field on how to obscure the data, so that attackers are unable to access it. This is part of what keeps the attackers out of your data, and makes sure your modern car's breaking systems hopefully cannot be disabled remotely. There exists many standardized algorithms and crypto systems today, which mostly does a seemingly good job. Crypto systems like AES and RSA are widely used and has yet to be broken. However, many of these traditional cryptography systems require a lot of computing power, energy consumption or memory. While these cryptography systems are suitable for home computers and servers, they may not be as suitable for all smaller devices. Devices like kitchen appliances, pacemakers and RFID-cards. After all, the latter devices will often have a very limited computing power, memory or energy supply. On some weaker systems, the algorithms may run slower than wanted. On others, it will not run at all. In addition to this, a lot of smaller, cheaper and weaker systems are more physically accessible to potential attackers. This can allow attackers a greater set of attack methods.

## Outline of the article

In this work, we give an overview of the lightweight cryptography landscape. We focus especially on IoT looking at symmetric ciphers and hashing algorithms. We look at specific details of the algorithms, like key sizes and implementation efforts. We list the merits and demerits for various algorithms, of how suitable they are for IoT.

Of many algorithms considered for analysis, we take a deeper look at Salsa20 [1], due to its recent success as a candidate for wider use. We focus on analysing the ease of attacks to supplement the existing studies analysing the attack possibilities. In this regard, we present an overview of attacks/cryptanalysis approaches. We formulate the main research question as follows:

- Does Salsa20 seem to be secure against existing attacks?
- Can we break a weakened version of Salsa20?

To answer these questions, we look at the state of the art of Salsa20 cryptanalysis in Section 2.6. We discuss some attack methods, and how some of these can be protected against. We also analyse the Salsa20 algorithm and one of its core components, the quarter-round $(Q R)$ function. We attempt two forms of analysis, each of them against both the full Salsa20 algorithm, and the Salsa20 quarter-round function.

The first of these methods, described in Section 3.3.3, is a differential analysis using the Hamming distance $(H D)$ for measuring distance between values. Here, we measure how the difference in multiple input values affect the difference in their output values. We do this both between an input and its output, and between two outputs with similar inputs.

The second method, described in Section 3.3.4, uses a deep learning tool called a context aggregation network, or CAN. It can be used to construct or modify images, based on data sets of input and output images. For more about CAN, see Section 2.7. Here, we encrypt plaintexts and image files. We generate images before and after the encryption, and train the network on them.

In the rest of this thesis, Chapter 2 presents the related background works, overview of the lightweight cryptography landscape relating to symmetric ciphers and hashing algorithms, overview of attack and cryptanalysis methods, how robust Salsa20 is against some of these methods and how some of the weaknesses can be reduced and protected against. In Chapter 3, we present a more detailed look into the structure of Salsa20, how its upgraded version ChaCha differs from it, and how we intend to analyse Salsa20 and its quarter-round. In Chapter 4 we discuss the results found when analysing the
algorithm. And finally, in Chapter 5 we draw conclusions from our results, and we discuss further work.

## Chapter 2

## Background

### 2.1 IoT and mesh network security

Due to the reduction of costs to produce microprocessors over time, their prevalence has risen drastically over the years (see [2]). Now, everything from cars to vacuum cleaners and coffee makers can be connected to the internet. While some purposes may not require high levels of security and performance, this still remains important for other systems [3]. There has also been a higher focus on mesh networks in later years, both in your home and outside. Traditional networks has had a main access point, like the router in our homes, which connects to all the devices in your home. This is what we refer to as a star topology, and is illustrated in Figure 2.1. This topology has a few advantages over mesh networks. For example:

- Only one main/hub device is needed, and
- it makes the networking structurally and topologically simple.

Since you need only a single device, it makes sense to put more effort and money into making it. Therefore, you can often make it with more processing power, more memory, etc. allowing for stronger crypto algorithms with higher requirements.

On the other hand, a router's reach is limited, and connecting multiple routers together to extend the signal, is often not a practical solution. In addition, if this one device fails, your network is down. This is where mesh networks become useful. Instead of having a single hub all other devices connect to, like routers or cell towers, you can have multiple nodes, with multiple devices connecting to each other. In Figure 2.2, we can see an illustration of how a mesh network can look like. Mesh networks can give the network a


Figure 2.1: Structure of a traditional star-formed network.
robustness that star topology networks will not be able to deliver. This topology can be used for everything from small 5G cell towers around the city, to IoT devices in your home. If one node or access point fails, the network can attempt to repair itself by re-adjusting and using other nodes [4] and connections. Mesh networks can thus be less likely to fail, as often multiple nodes has to break at once. The fact that nodes can carry the signal via each other means that the network range can be extended drastically, without requiring costly long-range routers. Mesh networks can even be useful in disaster areas, where the existing infrastructure has broken down, as discussed in [4] and [5].


Figure 2.2: Example of structure of a mesh network.
There are some important considerations here as well:

- The nodes are often more physically accessible than a single access point would be.
- The nodes are often afforded less security-related processing power than
a single main node would.
Basically, you have to trust the nodes in the network, which makes security potentially a more relevant issue than it already is. While a large cell tower on a hill may be inaccessible to most, a small 5 G node on a lamp post by your local street are easily more accessible.

Thus, to make IoT and mesh networks secure, they need to be protected against not only traditional attacks, but also physical side-channel attacks (see [6]). These are attacks not aimed only at the algorithm itself, but also the implementation of it. Using this kind of analysis, one can get access to more information about the encryption and decryption process, which can often be used to break otherwise strong algorithms. A deeper look into side-channel attack can be found in Table 2.11.

These technological advances make life more practical for millions of people, but it also has its downsides. A lack of proper cyber security can have negative and even fatal consequences. And yet many IoT products have a lax approach to security.

### 2.2 Basics of cryptography

In this Section, we talk about what cryptography is, what kinds of cryptography algorithms are used today, and they are used for. We talk about the two main categories of encryption algorithms; asymmetric (also known as public key) crypto and symmetric crypto, but we mainly focus on the symmetric side. We also look at hashing functions, and what they are used for.

When discussing ciphers and their strengths, words like confusion and diffusion is used a lot. It can therefore be good to understand the terms. Basically:

- Confusion obscures the relationship between the ciphertext and the key. Each ciphertext bit should depend on multiple parts of the key.
- Diffusion obscures the relationship between the ciphertext and the plaintext. If we change a bit of the plaintext, we should expect about half of the ciphertext bits to change, statistically speaking.


### 2.2.1 Encryption algorithms

Modern encryption can be split into symmetric and asymmetric algorithms Symmetric algorithms uses the same key $k$ for encryption and decryption. Asymmetric, on the other hand, uses a pair of related keys $\left(k_{1}, k_{2}\right)$. One for encryption, the other for decryption.

## Symmetric cryptography

Symmetric algorithms use the same key for encryption and decryption. This means that, when using symmetric key cryptography in communication, the key has to be known by both parties.

Symmetric ciphers can be defined by the functions $(E, D)$, where:

- $E$ is the encryption algorithm.
- $D$ is the decryption algorithm.
over the sets $(K, M, C)$, where:
- $K$ is the set of possible keys $k$.
- $M$ is the set of possible plaintext messages $m$.
- $C$ is the set of possible ciphertexts $c$.

The encryption and decryption algorithms are defined as follows:

$$
\begin{aligned}
& E: K \times M \rightarrow C \\
& D: K \times C \rightarrow M
\end{aligned}
$$

where the $\times$ symbol means the function $E$ maps $K$ and $M$ to $C$ (for the first line).

The defining element in symmetric algorithms, compared to asymmetric ones, is that encryption and its respective decryption uses the same key $k$, such that:

$$
\begin{aligned}
E(k, m) & =c \\
D(k, c) & =m
\end{aligned}
$$

And the following should therefore be true of symmetric encryption:

$$
D(k, E(k, m))=m
$$

Modern symmetric ciphers are generally split into two categories: Stream ciphers and block ciphers. The difference between these can be somewhat blurry, but generally, block ciphers encrypt the data in larger blocks, while stream ciphers encrypts 1 byte or bit at a time, usually by XORing them with the generated keystream. These are again built on different structures, as can be seen in Table 2.1. Stream ciphers often output ciphertext part by part, as the data is encrypted. They contain a hidden state which changes during the encryption, that are used for the generating the keystream (see [7]). Block ciphers requires larger chunks of the data to be encrypted before outputting
any of it. One of the good things about stream ciphers is that they can output data as soon as it is encrypted. When one byte or bit is encrypted, it can be sent on to the next process. Block ciphers has to wait for the entire block to be encrypted. This means they have to, at the very least, store an entire block in memory. For this reason, block ciphers often require more memory. Stream ciphers often use simpler cipher structures and require less hardware complexity (see [8]), thus making them more suited for cheap devices with low computing power and little memory. While stream ciphers has some upsides, they also often have a lot less, if any, diffusion. Remember from earlier that the diffusion of an algorithm is how well it obfuscates the relationship between the plaintext and ciphertext. Changing a single bit in the plaintext would also change a single bit in the ciphertext, assuming the keystream is not affected by the plaintext. Thus a lack of diffusion and a bad avalanche effect for the plaintext. While this does not mean block ciphers are more secure than stream ciphers, it does mean block ciphers can have an advantage here.

| Structure | Description |
| :---: | :---: |
| Iterated block ciphers | The idea of iterated block ciphers are to start with a block of plaintext of a certain size, and encrypt into a block of ciphertext of the exact same size. This is done by iterating the block through a number of rounds of encryption. These can generally be made secure by simply using a sufficient amount of rounds. |
| SPN | A Substitution-Permutation Network is an encryption scheme which first substitutes a specific amount of bits with another set of bits using S-boxes (look-up tables), then permutes, or shuffles, the values. This is usually done multiple times. The size of the S-boxes, the complexity of the permutation stage, the amount of rounds and the size of the full key are important factors to how secure such a structure is. For example, AES uses 8 bit S-boxes, shifts rows and columns, 10-16 rounds and 128-256 bit keys, while PRESENT, which is similar to AES, has 4 bit S-boxes, similar permutation, 31 rounds and $80-128$ bit keys. The larger amount of rounds attempts to make up for the smaller S-box [2]. More about this in Table 2.4 and 2.7. On the other hand, large S-boxes can quickly become an issue when attempting to construct small implementations [9]. |
| ARX | Modular addition, rotation and XOR. This type of structure changes the internal state first by modular addition between parts of the state. Next stage is rotation, usually through shifting bits a set amount of times. Finally, XOR between parts of the internal state. These hardware and software required for operations are relatively cheap and fast, which is part of what makes them popular (see [10] and [10]). |
| Feistel | Here, the plaintext is split into two halves of the same size. One of the halves are run through a round function and is XORed with the other half. This output is then stored on the other half. The two halves are then swapped, and this is repeated multiple times. |
| LFSR | Linear feedback shift register is a structure where the output of the next bit is affected by the previous bit. One of the good things about LFSRs are that they can be relatively small and simple. One of the big downsides of LFSRs are their linear nature, which makes them easy to attack. They should therefore be combined with non-linear elements to reduce this vulnerability. |

Table 2.1: Types of cipher structures.

## Asymmetric cryptography

The basic concept of asymmetric, or public key crypto, is that different, but related keys are used to encrypt and decrypt data. Using similar definitions to the symmetric encryption definition, where $E$ is an encryption algorithm, $D$ is its decryption algorithm, $m$ is the message, and $k_{0}$ and $k_{1}$ are the keys, we get the following.

$$
\begin{aligned}
E\left(k_{0}, m\right) & =c \\
D\left(k_{1}, c\right) & =m
\end{aligned}
$$

Put them together, and this should be true for asymmetric encryption.

$$
D\left(k_{1}, E\left(k_{0}, m\right)\right)=m
$$

In this case, $k_{0}$ would be the public key and $k_{1}$ would be the private key. Methods like Diffie-Hellman and RSA are based on the integer factoring problem. The factoring problem, relating to integer factorization, is the question of whether integer factorization can be solved in polynomial time on a classical (non-quantum) computer. This problem is considered to be hard complexitywise. Basically, this means that it takes a lot of effort to factorize a number into its primes. Say a number $a$, is made by multiplying two prime numbers $p$ and $q$. Finding $a$ is easy when you know $p$ and $q$ :

$$
p \cdot q=a
$$

Similarly, finding one of the primes, when we know $a$ and the other prime, is easy using division. For example, knowing $p$ and $a$, we can find $q$ as follows:

$$
\frac{a}{p}=q
$$

On the other hand, when only $a$ is known, finding the primes is very time consuming. Many types of asymmetric cryptography systems are based on this, or other hard problems.

Another type of asymmetric algorithm is the elliptic curve cryptography algorithms (ECC). (Not to be confused with error-correcting code.) ECC relies on the fact that it can be very difficult to create inverse functions of certain iterated mathematical functions, over elliptic curves. They can often use short key lengths compared to other forms of asymmetric cryptography.

Many of the asymmetric algorithms are much slower or require much more computation or memory, than symmetric algorithms. For this reason, they are often just used for key exchange. Due to this, asymmetric algorithms are generally used to encrypt keys for the symmetric cryptography, which can
then do the heavy lifting, so to speak. This is important for which kinds of algorithms are the most relevant for which part of networks. Especially when it comes to low-power and weak systems, which require more lightweight cryptographic algorithms.

Asymmetric algorithms may see a large shift in the future, as many of them are vulnerable to strong quantum computers (see [11] and [12]). Most asymmetric algorithms, unlike most symmetric algorithms, rely on the hard mathematical problems of integer factorization, discrete logarithm problem or elliptic-curve discrete logarithm problem. These are hard problems on classic computers, but much less so on quantum computers. While certainly interesting, post-quantum cryptography is not within the scope of this article.

## Relevance to the thesis

In this study, we mainly look at symmetric key cryptography, and not asymmetric (public-key) cryptography. Part of the reason for this is that to achieve sufficient security with many popular public-key crypto, like RSA, much larger keys are required (see [13] and [14]). We considered symmetric cryptography would be the field we could contribute knowledge to the most, largely due to the author's previous knowledge of symmetric cryptography, from university and online courses.

### 2.2.2 Hashing algorithms

In addition to looking at lightweight block and stream ciphers, we also looked at hashing algorithms. Hashing algorithms are useful in many situations. They can be used to authenticate messages by sending along a hash of the message, showing the message has not been changed. This is similar to how MAC/MIC (Message Authentication/Integrity Code) functions work. Indeed, some MACs are built on hash functions. They can also be used as components of encryption algorithms, like Salsa20, which uses a hash function for generating its sub-keys. Hashing can be used to "store" passwords in password databases. In some ways, especially relating to passwords, hashing algorithms can be viewed as a deterministic one-way encryption. When a server checks your password, it has not actually stored your password for comparing. Not in plaintext, nor as an encrypted password. It only stores the hash of your password. That is, the output of the hashing algorithm, when your password is the input. When you log in next time, your password is hashed again, and the server can compare the hashes. Since they are deterministic, the hash will always be the same.

$$
p w_{a}=p w_{b} \quad \Longrightarrow \quad \operatorname{hash}\left(p w_{a}\right)=\operatorname{hash}\left(p w_{b}\right)
$$

This way, servers can, in a sense, store your password without worrying as much about leaking or disclosing the passwords. Note that this is a bit of a simplification, as they should also use a salt when hashing, and maybe hash the password multiple times. Salting is done by adding another, preferably random, element into the hashing algorithms. That way, if two people have the same password (which is a very common occurrence), their hashes will be different, because their salts were different.

A hashing algorithm maps an input of arbitrary length $n$ to an output of fixed length $m$ :

$$
\begin{equation*}
\mathbb{F}_{2}^{n} \longrightarrow \mathbb{F}_{2}^{m} \tag{2.1}
\end{equation*}
$$

The digest size of the hashing algorithms is then $m$. So whether we hash a single letter, or a massive video file, the output will always be of size $m$. One of the natural consequences of the change in the size from $n$ to $m$ is that when $n>m$, we get collisions, due to the pigeonhole principle. This principle states that when mapping $n$ elements into $m$ containers, where $n>m$, there will be at least one container containing multiple elements. This can of course also happen if $n \leq m$, but it is certain when this is not the case. A collision is when both $a$ and $b$ results in the same hash output.

$$
\operatorname{hash}(a)=\operatorname{hash}(b)=c
$$

In this case, $a$ and $b$ causes a collision. In the case of passwords, a login server may consider them equal. For example, if the passwords "a_strong_password" and "abcd" both result in the hash "ac6a7b8"

$$
\operatorname{hash}(\text { a_strong_password })=\operatorname{hash}(\text { abcd })=\operatorname{ac6a} 7 \mathrm{~b} 8
$$

the server would accept either as the correct password. Frequent collisions would thus drastically weaken passwords checking and other uses of hash functions. Guessing passwords or keys can be hard, but if there are millions of different passwords, all of which are accepted, the change of guessing one of them is drastically better. How strong a hashing algorithm is against collisions depends on how large the digest is, and how well distributed the mapping is. The digest size is the output size of the hash function, as shown in Equation 2.1. With a small digest, collisions are more likely to find. If the digest size is 2 bits, then any hash will land in one of 4 hash values, and a brute force attack should be simple. With a digest size of 1024 bits, there are $2^{1024}$ values to land in, and, assuming a well distributed mapping, a brute force attack would impractical. Not all hashing algorithm are as good at mapping evenly distributed hashes though. If a hypothetical algorithm only maps to half of the output values, this practically halves the digest space, and makes collisions twice as likely.

### 2.3 Lightweight cryptography

As processing becomes more ubiquitous, and everything is being connected to networks, the need for security increases. The rise of smaller and often weak microprocessors, is problematic when most of the cryptographic algorithms of today are focused on servers, home computers and smart phones (see [15]). Some IoT systems are too weak to run existing public-key systems like RSA, or existing symmetric cryptography standards like AES (Advances Encryption Standards). Some may be able to run them, but not at sufficient speed. This separation between traditional algorithms and lightweight algorithms has grown [3]. The attempt to find solutions that are much smaller, simpler and lighter, while being as secure, or at least sufficiently secure for their purpose, is now more important than ever. Both NIST and ISO are working on guidelines and standards on lightweight cryptography (see [15] and [16]). Some also consider the lightweight field to be too big, and propose it should be split into two sub-fields (see [2], [13] and [17]):

- Ultra-lightweight crypto
- IoT-crypto

Under this categorisation, ultra-lightweight cryptography focus on things like crypto solutions in RFID cards, pacemakers and similarly very weak systems. These would usually be hardware implementations. IoT-crypto would focus more on implementations on strong microprocessors, where there is sufficient resources to have software abstractions and memory usage. By resources, we mean the amount of computational power, memory, energy, and such. Thus the cryptography field could be split into roughly three fields, based on and sorted by levels of resources available:

- Traditional cryptography
- IoT cryptography
- Ultra-lightweight cryptography

When designing or analysing a cryptography system, one can use three general factors (see [2], [16] and [17]), and how they affect each other:

- Security
- Cost
- Performance (speed)

As illustrated in Figure 2.3, each of these factors tend to affect the others. More security, for example by having more rounds or larger key lengths, means that performance and/or cost are often negatively affected. A well-parallelized crypto system may have better performance over a serialized one, but it will also require more space and/or stronger processors. The cost factor is also strongly related to the level of lightweight of the system. If an algorithm requires a powerful and expensive processor, some companies may cheap out Expensive systems will also not be very useful for RFID tags or extremely cheap IoT equipment. There are of course many more factors one can list, such as power and power consumption (see [2] and [13]), but this triad works as a good model.


Figure 2.3: Design trade-offs in lightweight cryptography.

### 2.4 State of the art - Lightweight cryptography

This work is mainly based on the works of Poschmann [2], Biryukov and Perrin [3], Eisenbarth, [18] the EU ECRYPT's eSTREAM [19] and the University of Luxembourg's CryptoLUX Wiki [20]. Other references are cited in the tables.

The eSTREAM portfolio is a set of 7 ciphers, chosen in the eSTREAM project from 2004 to 2008 [19]. The algorithms, as seen in Table 2.2, are split into software and hardware algorithms.

An introductory explanation of a lot of the terms used in the tables can be found in Table 2.3. In Table 2.4, 2.5 and 2.6, we show technical information about the block ciphers, stream ciphers and hashing algorithms respectively In Table 2.7, 2.8 and 2.9, we list up their general pros and cons, as well as known attacks (in the same order as with the technical information). Note that more known attacks does not necessarily imply weaker algorithms, or that they

| Profile 1 (SW) | Profile 2 (HW) |
| :---: | :---: |
| HC-128 | Grain v1 |
| Rabbit | MICKEY 2.0 |
| Salsa20/12 | Trivium |
| SOSEMANUK |  |

Table 2.2: eSTREAM portfolio.
are considered insecure. Known possible attacks are not necessarily practical attacks. In the example of AES-256, a related-key attack using a chosenkey distinguisher by Biryukov, et al., achieves a total complexity of $2^{131}$ time and $2^{65}$ memory (see [21]). For a description on what a related-key attack is, see Table 2.10. This, while being much more effective than a brute-force attack, is still very much impractical, and AES is thus still considered secure. AES is also more popular, so there has been more research into potential attack methods than other algorithms. Similarly, a lack of pros/cons does not imply the algorithm is perfect, but rather that there are no clear, outstanding positive/negative sides with the algorithm.

| Term | Explanation |
| :---: | :---: |
| SW and HW | SW and HW is short for software and hardware. This section is simply to tell whether the algorithm was made mainly for implementations in software, hardware or either. Of course, any algorithm can be made in both software and hardware, but some are more specialized for one or the other. |
| Key length | All symmetric ciphers use a cryptographic pseudorandom key. This is, put simply, a password used to encrypt and decrypt. How secure a key is depends on its level of entropy. Roughly speaking, how random it is and how long it is. As long as the keys are sufficiently random, the most important security characteristic of the key is its length. The longer the key, the bigger numerical space you will have to go through to guess the right one. On the other hand, longer keys means more storage required, and often more processing needed. Thus, longer keys are stronger but can also be less lightweight. |
| Block size | Block ciphers encrypt the data in blocks. Having large blocks may also be positive from a security standpoint. Having larger blocks also means more data will have to be stored, which is negative from a lightweight perspective. |
| Rounds | Most ciphers iterates a certain process multiple times. Some of the ciphers' rounds are stronger than others, but generally: More rounds means more secure, but also takes longer time. |
| Area (GE) | The GE, or gate equivalent, of an implemented algorithm says something about how large the algorithm has to be. Some are much smaller than others, which is of course positive for its lightweightness. Some have ranges, as it depends on how you implement your algorithm. For example, AES can be implemented without storing most of the S-boxes, and just generating them on the fly. This means a lot less storage, and thus a lot less GE and lower hardware requirements. On the other hand, having to generate the relevant parts of the S-box every time is slower. |
| Structure | As discussed earlier, ciphers can be based around different kinds of structures, with their own benefits and drawbacks. See Table 2.1 for more about this. |
| IV | IVs, or initialization vectors, are vectors use to initialize a state in a cipher. Some ciphers depend heavily on their internal state, and the IVs are there to ensure a proper initial state. The smaller the IV, the less memory required. On the other hand, where IVs are important, reducing their size or complexity may weaken the algorithm. |
| IS | The internal state is the temporary data in the algorithm, as it is processing data or keys. This has a certain size, and this size is important for the lightweightness of the algorithm. If it requires a large internal state, it will require more area, code size or memory. On the other hand, if the internal state is too small, the security of the algorithm may be compromised. For example, with a sufficiently small IS space, one may be able to guess the entire internal state. Therefore, most ciphers have an IS bigger or equal to their key size. |
| Digest size | A hashing function maps a variable amount of bits into a fixed size. This fixed size is the algorithm's digest. |
| Rate | The rate of a hashing algorithm is the size of the block being created each iteration. |

Table 2.3: Explanation of terms used in the state of the art analysis.

| $\#$ | Algorithm | HW/SW | Key length | Block size | Rounds | Area (GE) | Structure |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | AES | Both | $128 / 192 / 256$ | 128 | $10 / 12 / 14$ | 3100 | SPN |
| 2 | PRESENT | Both/HW | $80 / 128$ | 64 | 31 | $1075-1884$ | SPN |
| 3 | RC5 | - | $0-2040$ | $32 / 64 / 128$ | 12 | - | ARX |
| 4 | Chaskey | SW | 128 | 128 | $8 / 12 / 16$ | - | ARX |
| 5 | TWINE | Both | 128 | 64 | 36 | $1800 / 2285$ | GFN |
| 6 | SPARX | - | $128,128 / 256$ | 64,128 | $24,32 / 40$ | - | SPN (ARX) |
| 7 | SPECK | SW | $32-128$ | $64-256$ | $22-34$ | $884-1396$ | ARX |
| 8 | SIMON | HW | $32-128$ | $64-/ 256$ | $22-34$ | $763-1317$ | Feistel |
| 9 | PRINCE | - | 128 | 64 | 12 | $3286 / 3491$ | SPN |

Table 2.4: Technical information of block ciphers.

| $\#$ | Algorithm | HW/SW | Key length | IV | IS | Area (GE) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | A5/1 | - | 64 | 0 | 64 | - |
| 2 | ChaCha20 | SW | $128 / 256$ | 64 | 512 | - |
| 3 | E0 | - | 128 | 0 | 128 | - |
| 4 | F-FCSR-16/-H v3 | - | $128 / 80$ | $128 / 80$ | $256 / 160$ | - |
| 5 | Grain | HW | $80 / 127$ | 64 | 36 | $1294-4617$ |
| 6 | Mickey v2 | HW | 128 | $0-128$ | $200 / 320$ | - |
| 7 | Salsa20 | SW | 256 | 64 | 256 | - |
| 8 | SNOW 3G | - | 128 | 128 | 576 | - |
| 9 | Trivium | HW | 80 | 80 | 288 | - |

Table 2.5: Technical information of stream ciphers.

| $\#$ | Algorithm | HW/SW | Digest size | Rate | IS | Area (GE) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Armadillo | - | $80 / 127 / 160 / 192 / 256$ | $48 / 64 / 80 / 96 / 128$ | $256 / 384 / 480 / 576 / 768$ | $2923-11915$ |
| 2 | DM-PRESENT | - | 64 | $80 / 128$ | 64 | $1075-1884$ |
| 3 | GLUON | SW | $128 / 160 / 224$ | $8 / 16 / 32$ | $136 / 176 / 256$ | - |
| 4 | Lesamnta-LW | SW | 256 | 128 | 256 | - |
| 5 | PHOTON | - | $80 / 128 / 160 / 224 / 256$ | $16 / 32 / 36$ | $100 / 144 / 196 / 256 / 288$ | $1800 / 2285$ |
| 6 | QUARK | HW | $136 / 176 / 256$ | $8 / 16 / 32$ | $136 / 176 / 256$ | - |
| 7 | SipHash-2-4 | - | 64 | 64 | 256 | $884-1396$ |
| 8 | SPN-Hash | - | $128 / 256$ | $256 / 512$ | $128 / 256$ | $763-1317$ |
| 9 | Spongent | - | $80 / 128 / 160 / 224 / 256$ | $8 / 16$ | $88 / 136 / 176 / 240 / 272$ | $3286 / 349$ |

Table 2.6: Technical information of hash functions.

| \# | Pros |
| :--- | :--- |
| AES is the most common and stan- |  |
| 等 | dardized symmetric cryptography al- |
| - gorithm, and has been for a while. |  |
| Its prevalence means it has been well |  |
|  | tested and should be relatively strong. |

 PRESENT is very similar to AES. It
has a smaller s-box than AES (4-bit vs 8 -bit). It is very compact, at about 2.5 times smaller than AES (see [2]). This is a big advantage for its lightweightness.

| 号 |
| :--- |
|  |
|  |

RC5 is a simple algorithm, and has a When using fewer rounds (12, 64-bit variable block size, key size and rounds. blocks), it is susceptible to differenThat way it is more compatible with smaller implementations, which may need less security and less space.

## Cons

AES is difficult to make lightweight, and especially ultra-lightweight [22]. Among other reasons, because its large 8-bit s-box (substitution box), needing a lot of memory. It was not designed for (ultra)lightweight tasks.

## Attacks

- Impossible differential
- Related-key boomerang
- Biclique
- Chosen-key distinguisher [21]
- Statistical saturation
- Multidimensional linear
- Truncated differential
- Differential attack
- Linear attack
- Differential-linear
- Biclique (full cipher)
- Zero-correlation
- Integral

Related to Simon. Optimized for soft- Developed by the NSA. Does not have ware implementations [26]. good resistance against known-key attacks, as this was not thought of as that important for IoT crypto.
Related to Speck. Optimized for hardware implementations [26].

- Differential
- Rectangle

Developed by the NSA. Does not have good resistance against known-key attacks, as this was not thought of as that important for IoT crypto.

- Differential
- Linear
- Impossible differential
- Multidimensional linear
- Reflection attack
- Sieve-in-the-middle
- Multiple differentials

Table 2.7: Pros and cons of block ciphers.

| \# | Pros | Cons | Attacks |
| :---: | :---: | :---: | :---: |
| $\stackrel{+}{4}$ | Used in GSM. Wide usage often, though not always, implies good security, as they have generally been tested (and attempted broken) more. | Small key size, allows for practical attacks. A5/1 is broken. | - TMD trade-off |
|  | Variant of Salsa20, which is part of the eSTREAM winners. Has a modified round function, which is supposed to raise the diffusion, without affecting performance. |  | - Differential attack |
| 呈 | Widely used as it is used in Bluetooth. | Multiple known attacks which are more efficient than brute-force, though they are seemingly not sufficiently more efficient to be practical. | - Conditional correlation |
|  | Non-linearly updated FSRs. Provably safe after a certain amount of iterations. | Allows for a significant amount of collisions during the first clockings, before the main cycle is reached. | - |
| تٌ | Part of the eSTREAM winners. Based on two different FSRs, where their clocking affects each other to achieve non-linearity. |  | - Linear approximations <br> - Dynamic cube testers |
|  | Part of the eSTREAM winners. |  | - Entropy loss <br> - Weak keys |
| $\begin{aligned} & \text { N్ } \\ & \text { W } \\ & \text { N } \\ & \tilde{\sim} \\ & \text { N } \end{aligned}$ | Part of the eSTREAM winners [19]. No published attacks as of 2015. Secure against timing side-channel attacks. | Weak against some types of sidechannel attacks (see [27] and [28]). Lacks research into its security (see [29]). | - |
|  | Chosen by the 3GPP consortium. [30] | Uses the (large) AES S-box. | - Multiset distinguisher |
|  | About: Block-stream-cipher. XORs with bits from an external source to reduce the need for a large S-box. Uses 3 internal LFSRs. There is also "Bivium", which uses only 2. <br> Trivium saves space due to the lack of a large S-box. | The external bits could be biased, and thus weaken the security of the algorithm. | - Algebraic (Bivium) <br> - Conditional differential |

Table 2.8: Pros and cons of stream ciphers.

| \＃ | Pros | Cons | Attacks |
| :---: | :---: | :---: | :---: |
|  | － | It is large and it has been broken． | －Local－linearization （practical） |
| － |  |  |  |
|  | Based on PRESENT，which is lightweight and fairly secure． | The small digest size makes it less col－ lision resistant． | －Multi－differential（colli－ sions： 12 rounds，distin－ guisher： 18 rounds） |
| $\begin{aligned} & \text { Z } \\ & \text { B } \\ & \text { 心. } \\ & \text { s } \end{aligned}$ | Based on FSCRs，which can be both good and bad． |  | －Iterated preimage attack |
|  | Reuses AES－elements，making it more secure． | Reuses AES－elements，making it larger and less lightweight． | －Integral |
|  | Inspired and based on PRESENT and AES，which seems like a pretty LW and secure algorithm．Reuses from AES or PRESENT based on need． | － | － |
| $\begin{aligned} & \text { 令 } \\ & \text { 心́ } \\ & \dot{0} \end{aligned}$ | Hardware oriented and fast． | － | － |
|  |  | Not collision resistant（due to small di－ gest size）．Large． | － |
|  | Probable security against differential collision attacks．Based on an AES－like SPN． | Similar issues as other AES－based sys－ tems．Large． | － |
|  | Based on a modified version of PRESENT．No known successful at－ tacks on Spongent． |  | －Linear distinguishers |

Table 2．9：Pros and cons of hashing algorithms．

### 2.5 Cryptanalysis

Through the years, many types of attacks has been used and proposed against different kinds of cryptographic algorithms. This section will go through some of these, with the main focus being on symmetric ciphers.

Firstly, what kind of attack can be used depends on how much information the attacker has access to. For a list of types, see Table 2.10.

| Knowledge | Description |
| :--- | :--- |
| Cipher-text only | Here, the attacker only has access to <br> the cipher-text. The attacker knows <br> nothing about the key, the plain- <br> text/data, etc. |
| Chosen plain-text or <br> cipher-text | In this case, the attacker can chose <br> the plain-text or cipher-text. This <br> may allow them to change it to as- <br> certain more information about, for <br> example, the key. |
| Known plain-text | In this case, the attacker knows the <br> plain-text, but has not, and can not, <br> choose the plain-text themselves. |
| Adaptive chosen | Here, the attacker decides the plain- <br> text and can change it as they will. |
|  | The attacker can for example look <br> for differences in cipher-text based <br> on differences in plain-text. |
| Related-key attack | Sometimes keys are related, and <br> here, the attacker can know the re- |
|  | lation, without necessarily knowing <br> the keys. |

Table 2.10: Amount of knowledge the attacker has access to.
Usually, the attacker wants to find the key or the plaintext. Of course, finding one can often make finding the other rather simple. In the cryptography community, it is well accepted that one should always expect the attacker to know everything about the algorithm. Hiding the algorithm, while maybe making it somewhat more difficult to crack, is usually not a sufficient defense against attacks. Many older algorithms, made as in-house crypto solutions, have later been analysed, leaked or disclosed, decompiled, etc, and subsequently cracked (see [3]). This is related to whether algorithms and their cryptanalysis should be public and open-source. When algorithms are closed-
source, it may be better hidden from attackers, and thus harder for attackers to analyse. On the other hand, they are therefore often analysed less by security experts, and it is less likely that potential security holes are found. This is why open-source crypto algorithms are the expected norm these days.

To break algorithms, you often need a large amount of one or more of the following:

- Time
- Data
- Memory

In a simple brute-force attack, where all key combinations are checked, you will need a lot of time. This is usually on "the age of the universe" time scales, as the key search space is vast. On the other hand, if some form of adaptive chosen plain-text attack is attempted, a huge amount of data may be needed. Similarly, sometimes it is needed to store large amounts of data.

Sometimes, one can achieve only a partial attack, or an attack where some knowledge is found, but not all. As an example, modern algorithms attempt to make the ciphertext indiscernible from random noise. If one can implement an attack or analysis which is able to distinguish between random noise and the ciphertext from an algorithm, one may be able to use that in a more complete break. This is known as a distinguishing attack. In other cases, one may be able to retrieve information about a hidden closed-source algorithm, and use it to rebuild a functionally equivalent algorithm.

In Table 2.11 we can see a list of many types of attacks. Some more general than others. This is not a comprehensive list, but gives an insight to the cryptanalysis landscape for symmetric ciphers.

| Attack type | Description |
| :--- | :--- |
| Brute-force attack | This is the simplest type of attack. Essentially try all of the combinations. This is <br> generally the worst case scenario in a break. This is what you do with a bike lock <br> you have forgotten the key/password for. Works great for bike locks, phone locks <br> (without hardware-blocking for too many attempts) and bad (short) passwords. <br> When using 128 bit keys, on the other hand, it takes too long to be practical. |
| Differential analysis | This kind of attack analyses how changes in the input affects the output. What <br> happens with the output of the algorithm when a single bit is changed in the <br> key? If one can find patterns in the differences here, one may be able to recover <br> the original key, for example by using hill climbing algorithms. |
| Distinguishing at- |  |
| tack | This kind of attack or analysis attempts to find separate the ciphertext from <br> random noise, and uses that to attack the algorithm. |
| Boomerang attack | The boomerang attack is a type of differential attack primarily used for breaking <br> block ciphers. This enables us to attack specific parts of the block cipher. |
| Integral cryptanaly- |  |
| sis | This is mostly relevant against SPN networks. Using multiple sets of pairs of <br> related chosen plain-texts, where only parts of the plain-texts are differing from |
| reach other, while most of the bits remains the same. This is also knows as the |  |
| each |  |
| square attack, and is similar to the saturation attack. |  |

Table 2.11: Cryptanalysis techniques and attacks for symmetric ciphers.

### 2.6 Cryptanalysis of Salsa20

We looked deeper into the security of Salsa20, and how much research there is on attack methods. This work focuses on the Salsa family, partly because Salsa algorithms has been adopted in multiple important standards and software solutions, and partly because some studies indicate a lack of security research (see [31]). The discussed analysis and attack methods can be found in Table 2.12. We found that the most realistic attacks seems to be the ones where we assume knowledge from side-channel analysis, to perform cryptanalysis on Salsa20.

We also looked a bit at a few relevant methods to protect against sidechannel attacks, which can be seen in Table 2.13.

### 2.7 Context aggregation networks

We used a context aggregation network, or CAN, for parts of our research. This section talks a bit about what that is.

Deep learning is a form of machine learning based on artificial neural networks (ANN), using multiple layers for extracting features from raw input data. These types of networks are used in fields like social networks, computer vision, natural language processing, speech recognition, biometrics, translation, and even winning quizes, like when IBM's Watson won the American quiz show Jeopardy (see [34]).

A context aggregation network is a form of deep learning network, built and based upon convolutional neural networks (CNNs). It was created in 2019 by W. Cheng. et al. for semantic labeling in aerial images (see [35] and [36]), and was applied in various other applications. We were unable to find any previous research into these networks being used for cryptanalysis.

| Attack type | Attack type description | Salsa20 vulnerability |
| :---: | :---: | :---: |
| Non-sidechannel attacks | Create a function, or set of functions, which always, often or sometimes give you knowledge about the key, regardless of implementation method. | Salsa20 seems to be relatively strong against these kinds of attacks, though there is a lack of research here. ChaCha seems even stronger, due to higher diffusion in its roundfunction. |
| Timing attacks | Measure how long the cache, server, device etc. uses to reply. If the algorithm takes different amounts of time based on the key (like size of the key, bits of the key, errors in the key, etc.), you can learn something about the key, and thus be able to reduce the search space. | Not affected. Salsa20 is constant-time independent of input, and thus gives the attacker no information. |
| Power attacks | Measure the power usage, or the EM radiation, of the circuit. By knowing the setup of the algorithm, you can find out where, for example, bits are added together, multiplied etc. Worst case scenario is that you can read out the key bits almost directly, by measuring when it performs a multiplication carry or not. | Salsa20 is relatively weak against these kinds of attacks, due to the kinds of operations it uses. (Word-addition, etc). |
| Bricklayer attack | Optimized attack based on a divide-and-conquer strategy (see [28]). | One of the attacks we looked at. This attack seems promising against weakened versions of Salsa20, like Salsa20/8. |

Table 2.12: Potential attacks against Salsa20.

| Method | Description | Effective against | Pros and cons |
| :---: | :---: | :---: | :---: |
| Masking | Obscure internal variables by splitting sensitive temp variables into a set amount (masking order +1 ) of parts. This requires generating pseudorandom numbers. | Most kinds of attacks [32]. | + Secure against most attacks [33]. - Often very expensive, and thus not an optimal solution for lightweight systems [33]. |
| Code poly-morphism | Hide code functionality from being read, by constantly changing the code [32]. Generating code variants statically (multiversioning) or at runtime (generates different code efficiently and periodically). Uses a bunch of different configurations to change the code here and there, making too many possibilities to brute force. Tools like Odo can be used in this regard [32]. | Runtime (most attacks, specified): <br> - Register shuffling <br> - Instruction shuffling <br> - Semantic variants <br> - Insertion of noise instructions | Statically: <br> Limited by the final size of the program, generating more variants induces an increase of code size. <br> Runtime: Runtime code generation is usually avoided in embedded systems due to the potential vulnerability of accessing memory with both write and execution permissions. |

Table 2.13: Some existing protection methods against cryptographic attacks.

## Chapter 3

## Methodology

The Salsa family consists of a set of stream ciphers. They were created by Daniel J. Bernstein, and they are widely used. They can be found in the eSTREAM portfolio [19] and in the TLS cipher suites [37].

In this section, we look at the construction of Salsa20 and how its updated version ChaCha differs from the original. Salsa20 is built on an ARX structure, and so first, we discuss what that is. We then run through a detailed description of how Salsa20 is constructed, and of how ChaChas design differs. Finally, we look at our methods of analysis.

### 3.1 Detailed description of Salsa20

### 3.1.1 ARX

Salsa20 is built using an ARX structure in its core. ARX is an abbreviation for modular Addition, Rotation, XOR (exclusive or). This section explains what each of these elements does.

## Modular addition

Modular addition addition is performed by adding two numbers together, and then reducing the result with a given (fixed) modulus. We denote modular addition with the symbol $\boxplus$. In the case of Salsa20, two 32 bit numbers are added into a third number. If this number requires more than 32 bits, we simply cut off the leading bits, and make it into a 32 bit number. In Equation 3.1, we can see an example of normal addition and modular addition:

$$
\begin{align*}
& 1001+1001=10010 \\
& 1001 \boxplus 1001=0010 \tag{3.1}
\end{align*}
$$

In line 1, we add two 4 bit numbers, resulting in a 5 bit number. In line 2, we add the same two 4 bit numbers, but reduce the result with modulus 4 . This results in a 4 bit number.

## Rotation/shift

The rotation, or shift, simply shifts the bits a set amount. In the case of the Salsa family, the shift is to the left. A shift of $n$ bits is denoted as $\ll n$. For example:

- abcdefg $\lll 3=$ defgabc
- $00000001 \lll 7=10000000$


## XOR

Finally, XOR, or exclusive or, is a Boolean operation, working as a bit-by-bit difference comparison. We use the symbol " $\oplus$ " to denote an XOR operation. If the two compared bits are different, the resulting bit is a 1 . Otherwise, it is a 0 . As an example:

$$
\begin{array}{r}
00110001 \\
\oplus 10001100 \\
=10111101
\end{array}
$$

### 3.1.2 Overview of Salsa20

Salsa20, like many other stream ciphers, is XORing the plain-text data with a sub-key keystream. This means the size of the keystream has to be the same as the size of the data or data block. This is much the same concept as a one-time pad (OTP). While OTPs are unbreakable, they are rarely used, as key exchange would be impractical (see [38]). Therefore, to keep the key at a reasonable size, Salsa20 has a pseudorandom generator (PRG), which uses an expansion function and hash function, to generate the keystream. This is illustrated in Figure 3.1. The task of this function is to have the key as well as the nonce, block number and IV, as input. It then expands the key to many, large sub-keys. Specifically, expand a 16 or 32 byte key into as many 64 byte sub-keys as needed to encrypt the data. This way, you will not have to send gigabytes worth of keys to be able to send large files. You will only have to send a small key, and Salsa20's expansion function will expand it. Since this function is expanding a seed into a set of pseudorandom numbers, it is essentially a pseudorandom generator (or PRG).


Figure 3.1: Overview of the structure of Salsa20.

Once a sub-key is created, it can be XORed bit-by-bit with 64 bytes of the unencrypted plain-text data. In the case of decryption, the cipher-text is XORed and you get back the plain-text. This can also be seen in Figure 3.1.

The PRGs 64 byte ( 512 bit ) input consists of the following:

1. Key (32 bytes).
2. IVs (16 bytes).
3. Cryptographic nonce ( 8 bytes).
4. Block/counter number (8 bytes).

The key, nonce (which we will define soon), block number and the internal initialization vectors (IV) are combined to make the internal state (IS). Salsa20 has two set of IVs; one for each key-size mode. These IV sets are defined as shown in Table 3.1 (see [1]).

| A | B |
| :--- | :--- |
|  |  |
| $0 .(101,120,112,97)$ | $0 .(101,120,112,97)$ |
| 1. $(110,100,32, \mathbf{5 1})$ | $1 .(110,100,32, \mathbf{4 9})$ |
| $2 .(50,45,98,121)$ | $2 .(\mathbf{5 4}, 45,98,121)$ |
| $3 .(116,101,32,107)$ | $3 .(116,101,32,107)$ |

Table 3.1: Salsa20's initialization vectors (IVs).
The differences between A and B are highlighted with bold text. Running these numbers through an ASCII conversion table, we get the IVs as "expand 32-byte k" for IV A ( 32 byte key) and "expand 16-byte k" (16 byte key) for IV B. The initial state (IS) of Salsa20 can be arranged as a $4 \times 4$ matrix. Table 3.2 shows the matrix for a 32 byte key (IV A), where the key cells contains 4 bytes of the key, the nonce cells contains 4 bytes of the cryptographic nonce, and the block cells contains 4 bytes of the block number.

| "expa" | key | key | key |
| :--- | :--- | :--- | :--- |
| key | "nd 3" | nonce | nonce |
| block | block | "2-by" | key |
| key | key | key | "te k" |

Table 3.2: Salsa20's initial state (IS) for 32 byte keys.
Salsa20 supports both 32 byte keys and 16 byte keys. These are managed as follows:

- When using a 32 byte key $\rightarrow$ Split the key $k$ into two sub-keys $k_{0}$ and $k_{1}$. Use IV A.
- When using a 16 byte key $\rightarrow$ Apply the key $k$ twice. Use IV B.

We can see how these different parameters are given to the hash function, in Equation 3.2. In this case, $k$ (line 2) is a 16 byte key, while $k_{0}$ and $k_{1}$ (line 1) are the two parts/sub-keys of a 32 byte key. Thus, the expansion function
receives the key or key bits, as well as the nonce. It calls the hash function with the split keys $\left(k_{0}\right.$ and $\left.k_{1}\right)$ or duplicated keys $(k)$, the nonce $(n)$ and the IVs as input parameters, totalling 64 bytes. The hash function returns 64 bytes of pseudorandom data. This data is then XORed with the initial input, and becomes the first sub-key. For more sub-keys, which are required when the data is bigger than 64 bytes, repeat the same process, but after incrementing the block number.

$$
\begin{align*}
\operatorname{Exp}_{32}\left(k_{1}, k_{2}, n\right) & =\operatorname{Hash}\left(a_{0}, k_{0}, a_{1}, n, a_{2}, k_{1}, a_{3}\right)  \tag{3.2}\\
\operatorname{Exp}_{16}(k, n) & =\operatorname{Hash}\left(b_{0}, k, b_{1}, n, b_{2}, k, b_{3}\right)
\end{align*}
$$

Here, Exp refers to the expansion function, Hash refers to the hash function, and 32 and ${ }_{16}$ refers to the size of the key in bytes.

A cryptographic nonce is usually a random number, which is used for a single encryption/decryption pair. This is to add even more randomness to the algorithm. It can also be based on hardware states, as is done in the stream cipher Trivium [39]. Ensuring the nonce is not reused is hard in lightweight crypto, as it either has to use non-volatile flash memory or base it on the hardware [40]. The block number is a binary number counting up for every block of data being processed in an encryption or decryption. So the first block of data will have block number $00 \ldots 00$, the second will have block number $00 \ldots 01$, etc. This ensures the initial state per block, is never the same, as long as the nonce is changed at least every $2^{64}$ blocks. Otherwise, the block number will overflow and return to $00 \ldots 00$, and this initial state will be used twice. Using the same hash input twice may allow an adversary to attack the algorithm.

The PRG, seen in Figure 3.1, consists of an expansion function, which then uses a hash function, which again uses the double-round function. The double-round function consists of 1 full round of the row-round function, and one round of the column-round function. Each of these functions again consists of 4 rounds of the quarter-round function, applied differently to the different parts of the IS. The quarter-round function ( $Q R$ for short) is performed a total of 80 times in Salsa20, and a reduced amount in Salsa20/12, Salsa20/8, etc. The $/ 8$ means a reduced form of Salsa20, with only 8 full rounds, rather than 20 .

The hash function receives a 64 byte input $\left(b_{0}, b_{1}, \ldots, b_{63}\right)$. It uses these to construct 16 words $\left(w_{0}, w_{1}, \ldots, w_{15}\right)$, each of 4 bytes. These are created using the Littleendian (Lit) function, which will be defined soon, as described
in Equation 3.3.

$$
\begin{gather*}
w_{0}=\operatorname{Lit}\left(b_{0}, b_{1}, b_{2}, b_{3}\right) \\
w_{1}=\operatorname{Lit}\left(b_{4}, b_{5}, b_{6}, b_{7}\right)  \tag{3.3}\\
\quad \ldots \\
w_{15}=\operatorname{Lit}\left(b_{60}, b_{61}, b_{62}, b_{63}\right)
\end{gather*}
$$

It then runs these words through the double-round (referred to as Dr) function 10 times:

$$
\left(z_{0}, z_{1}, \ldots, z_{1} 5\right)=\operatorname{Dr}^{10}\left(w_{0}, w_{1}, \ldots, w_{15}\right)
$$

Finally, the hash function combines all these by concatenating a series of Lit functions, as shown in Figure 3.4.

$$
\begin{gather*}
\operatorname{Lit}\left(z_{0}+w_{0}\right) \\
\operatorname{Lit}\left(z_{1}+w_{1}\right)  \tag{3.4}\\
\ldots \\
\operatorname{Lit}\left(z_{15}+w_{1} 5\right)
\end{gather*}
$$

The Lit function received 4 bytes, and changes their order. It does so as shown below:

$$
\operatorname{Lit}(b)=b_{0}+2^{8} b_{1}+2^{16} b_{2}+2^{24} b_{3}
$$

Note that the + symbols in this case implies concatenation, not addition or modular addition.

The double-round function consists of a row-round function and a columnround function, both of which are applied once during a double-round, as shown below:

$$
\operatorname{Dr}(x)=\operatorname{Rr}(\operatorname{Cr}(x))
$$

In this equation, Dr refers to the double-round function, $\operatorname{Rr}$ refers to the rowround function, Cr refers to the column-round function and $x$ is a 16 word input. The row-round and column-round both consist of 4 quarter-rounds. When placing the 16 words into a $4 \times 4$ matrix, as shown in Table 3.3 , the row-round function takes row by row, while the column-round function takes column by column.

In the illustration in Figure 3.2 we can see the ARX structure elements in the quarter-round. It consists of a set of modular additions, bit-shift rotation and XOR functions. The quarter-round function is invertible, as all of its operations are invertible. The Salsa20 $Q R$ function takes a 16 byte/128 bit $X$ as an input and outputs a 16 byte $/ 128$ bit $Y$. A full round performs 4 quarter-rounds, making sure all parts of the internal state is run through the

| $x_{0}$ | $x_{1}$ | $x_{2}$ | $x_{3}$ |
| :---: | :---: | :---: | :---: |
| $x_{4}$ | $x_{5}$ | $x_{6}$ | $x_{7}$ |
| $x_{8}$ | $x_{9}$ | $x_{10}$ | $x_{11}$ |
| $x_{12}$ | $x_{13}$ | $x_{14}$ | $x_{15}$ |

Table 3.3: The 16 binary words being used in the double-round function.


Figure 3.2: Flowchart of the Salsa20 quarter-round function.

QR function every round. The $X$ and $Y$ are split up in 4 pieces, each 4 bytes/32 bits, as shown in Equation 3.5.

$$
\begin{align*}
& X=\left[x_{0}, x_{1}, x_{2}, x_{3}\right] \\
& Y=\left[y_{0}, y_{1}, y_{2}, y_{3}\right]  \tag{3.5}\\
& x_{i}, y_{i} \in \mathbb{F}_{2}^{32}
\end{align*}
$$

The $Q R$ function can be written out as shown in Equation 3.6.

$$
\begin{align*}
& y_{1}=x_{1} \oplus\left(\left(x_{0}+x_{3}\right) \lll 7\right) \\
& y_{2}=x_{2} \oplus\left(\left(y_{1}+x_{0}\right) \lll 9\right)  \tag{3.6}\\
& y_{3}=x_{3} \oplus\left(\left(y_{2}+y_{1}\right) \lll 13\right) \\
& y_{0}=x_{0} \oplus\left(\left(y_{3}+y_{2}\right) \lll 18\right)
\end{align*}
$$

### 3.2 How ChaCha differs from Salsa20

ChaCha offers a solution to one of the potential issues in Salsa20's quarterround function. In the Salsa20 $Q R, y_{1}$ is affected by $x_{0}, x_{1}$ and $x_{3}$, but not $x_{2}$. On the other hand, $y_{0}, y_{2}$ and $y_{3}$ is affected by all of $X$. This means $y_{1}$ has less diffusion, and is thus weaker against potential attacks. ChaCha has updated this by using a modified $Q R$ function. It should diffuse more, as all output words are affected by all input words (see [41] and [42]). This is done without making it slower. In fact, in some cases it can improve speed and use less temporary memory (see [41]).

When describing the ChaCha quarter-round, we use slightly different notation than with Salsa20. Rather than $\left(x_{0}, x_{1}, x_{2}, x_{3}\right)$ as inputs and ( $y_{0}, y_{1}, y_{2}, y_{3}$ ) as outputs, we use ( $a, b, c, d$ ) for inputs, and we update them directly. This means implementations of ChaCha can save some memory, where Salsa20 would require storing temporary variables.

The ChaCha quarter-round is described in Equation 3.7. The operations are performed left to right and top to bottom, similar to how it would be programmed in C. An illustration of the ChaCha quarter-round function is shown in Figure 3.3.

$$
\begin{array}{lll}
a+=d, & d \oplus=a, & d \lll 16 \\
c+=b, & b \oplus=c, & b \lll 12  \tag{3.7}\\
a+=d, & d \oplus=a, & d \lll 8 \\
c+=b, & b \oplus=c, & b \lll 7
\end{array}
$$



Figure 3.3: Flowchart of the ChaCha quarter-round function.

### 3.3 Analysis on Salsa20

In this section, we describe our how we analyzed Salsa20 and its quarter-round function. We perform all analyses on both a full Salsa20 encryption and the quarter-round function. While breaking the quarter-round function is not very useful in and of it self, it is interesting to compare it with Salsa20. Our analyses should presumably perform better against the quarter-round function, than against Salsa20. We analyse 3 methods in this section:

- Brute-force attacks
- Hamming distance-based analysis
- CAN-based analysis


### 3.3.1 Test setup

First, we look at the brute-force attack. While a brute-force attack is guaranteed to be successful, it is also very ineffective and slow. We therefore estimate our implementation against a brute-force attack.

We implemented a test setup of Salsa20, which we used in this analysis (see [43]). It is built in Python 3.7, and was run on an Intel i7-4790k processor running Windows 10 (x64).

The CAN-based analyses were implemented in Matlab 2020b, based on a modified image processing tool from MathWorks. The same test setup from earlier, trained the models on a NVIDIA GTX 980 Ti. The rest was implemented in Python 3.7.

### 3.3.2 Brute-force estimation

## About brute-force attacks

The basics of a brute-force attack is to guess all of the possible values, until one works. Say the deterministic function $f$ takes input $A$ and returns and output $B$. We write this as $f(A)=B$. We guess or count new $A^{\prime}$ for all possible $A \mathrm{~s}$, where $f\left(A^{\prime}\right)=B^{\prime}$. Whenever the guessed and real output are the same, we can conclude either the inputs are the same, or that we have found a collision.

$$
B=B^{\prime} \quad \Longrightarrow \quad f(A)=f\left(A^{\prime}\right) \quad \Longrightarrow \quad A=A^{\prime}
$$

## Estimating how long a brute-force attack would take on our setup

We run tests on the Salsa20 $Q R$ function and the ChaCha $Q R$ function. We also run tests on the Salsa20 full encryption and decryption, using 32 byte ( 256 bit) keys. All of these tests were performed with random values. The results can be found in Table 3.4, where rate $=\frac{\text { runs }}{\text { time }}$.

| Function | Runs | Time (s) | Rate $(1 / \mathrm{s})$ |
| :--- | ---: | ---: | ---: |
| Salsa20 QR | 100000 | $10.472 \ldots$ | $9548.432 \ldots$ |
| ChaCha QR | 100000 | $9.784 \ldots$ | $10219.841 \ldots$ |
| Salsa20 encrypt | 100 | $7.261 \ldots$ | $13.771 \ldots$ |
| Salsa20 decrypt | 100 | $7.155 \ldots$ | $13.974 \ldots$ |

Table 3.4: Results from the speed performance test.
We can see how the Salsa20's and ChaCha's $Q R$ function run at roughly the same rate ( 10000 per second). Salsa20 encryption and decryption also run at roughly the same rate ( 14 per second).

Since the $Q R$ function takes a 128 bit binary number, the total possible combinations of inputs are $2^{128}$. A complete search would thus take about:

$$
\frac{2^{128} Q R}{10000 \frac{Q R}{s}}=3.4 \cdot 10^{34} s
$$

or about $10^{27}$ years. Assuming we can know the cryptographic nonce used, a complete search of the 256 bit key space would take roughly:

$$
\frac{2^{256} \text { runs }}{14 \frac{\text { runs }}{s}}=2.4 \cdot 10^{76} s
$$

or about $10^{68}$ years. While one could expect to find the correct Salsa20 key or $Q R$ input in about half of the time for a complete search, either are still very much impractical. We can thus conclude that a brute force attack on either the key or the $Q R$ input on either our Salsa20 or our ChaCha implementations is infeasible. While there are much faster and effective implementations of the Salsa algorithms, 128 bit keys and 256 bit keys are generally considered practically secure.

### 3.3.3 Hamming distance differential analysis

In this section, we look at a Hamming distance-based form of differential cryptanalysis.

## Hamming weight and Hamming distance

The Hamming weight $(H W)$ of a binary number is the amount of non-zero bits. So $H W(00100100)=2$, as the number has two 1's. The Hamming distance is the amount of bit-by-bit difference between two binary numbers. So $H D(1000,0000)=1$, as the first bit is different between the two numbers. This can be formulated into the following pseudocode, where $Q$ and $P$ are the two numbers, and bit_q and bit_p are the bits currently being compared.

$$
\begin{aligned}
H D= & 0 \\
\text { for } & \text { bit_q, bit_p in } Q, P: \\
& \text { if bit_q }=/=\text { bit_p: } \\
& \quad \text { increment } H D
\end{aligned}
$$

Since XOR also does a bit-by-bit difference check, we can alternatively write the $H D$ function as:

$$
H D(1000,0100)=H W(1000 \oplus 0100)=H W(1100)=2
$$

## Differential analysis

We take a random input $X$ and output $Y$, such that $f(X) \rightarrow Y$, where $f$ is the encryption function we attempt to analyse. We then modify $X$ into $X^{\prime}$, by flipping $n$ bits. Run it through the encryption function $f: f\left(X^{\prime}\right) \rightarrow Y^{\prime}$. The question now is, after $n$ flipped bits between $X$ and $X^{\prime}$, how many bits are flipped between $Y$ and $Y^{\prime}$ ? Or more specifically, if

$$
H D\left(X, X^{\prime}\right)=n \rightarrow H D\left(Y, Y^{\prime}\right)=m
$$

what is $m$ ? Does a static $n$ mean $m$ is also static? If not, what is its average value for different values of $n$ ? See Figure 3.4 for an overview of the analysis method. If we can use this to decide whether or not a random $X^{\prime}$ is close to


Figure 3.4: Algorithm for the differential HD analysis on $X-Y$ pairs.
$X$, by looking at the $Y^{\prime}$ and $Y$, we may be able to use this in an attack against the algorithm. We perform this analysis on both the Salsa20 quarter-round function, and on Salsa20's PRG.

If the algorithm has a good avalanche effect, you would expect the HD to be about the same as the HD between two random values: About half the bits. More formalised, if $Q$ and $P$ are two random binary numbers of length $n$, we would expect:

$$
H D(Q, P) \approx \frac{n}{2}
$$

This is our null hypothesis. If, however, what we see differs from this expected value, it illustrates a lack of proper avalanche effect of the function.

### 3.3.4 CAN analysis

In this section, we describe how we perform a known-ciphertext analysis using a context aggregation network, or CAN. Since these networks are made for creating or modifying images, we need to make the inputs and outputs into images. We attempted to make a CAN learn how to construct plaintexts from ciphertexts. We tried 2 different methods for doing this:

1. Using randomly generated plaintexts, through both Salsa20 and the quarter-round function.
2. Using existing images, through only Salsa20.

Once we had encrypted and unencrypted images, we can train the network on them, and measure how well it learns. We varied multiple settings for the training to see how it affected the learning process:

- Patch size: From $16 \times 16,32 \times 32.64 \times 64$ and $256 \times 256$.
- Initial learning rate: From 0.000001 to 0.1.
- RGB weights: 1 to 3 for all RGB values, 1 to 32 for filters.
- Leaky ReLU (Rectified Linear Unit) Layers: 0.1 to 0.6 .


## Random plaintext-ciphertext pairs

This analysis method uses sets of plaintext (PT) ciphertext (CT) pairs, converts them into images and trains the CAN on them. See Figure 3.5 for an illustration.


Figure 3.5: Algorithm for CAN analysis on PT-CT pairs.

In this approach, we generated 5 sets of binary pairs, each containing a million pairs. These are shown in Table 3.5.

When these sets of pairs were generated, they were converted graphical images. One set of images for the plaintexts and one set for the ciphertexts. To

| Encryption <br> algorithm | Size <br> (bits) | Generation method |
| :--- | ---: | ---: |
| Salsa20 | 1024 | Converted incrementally larger numbers <br> $(0,1, \ldots, 1000000)$ to binary. Padded to fit <br> size requirement, and encrypted. See Figure <br> 3.6 for a pair from this set. |
| Salsa20 | 1024 | Generated random binary numbers of size <br> 1024, and encrypted them. See Figure 3.7 <br> for a pair from this set. |
| QR function | 128 | Generated random binary numbers of size <br> 256, and encrypted them. |
| None | 1024 | Generated two random binary numbers of <br> size 1024. No encryption. These are used <br> for comparison to the encrypted pairs. |
| None | 128 | Generated two random binary numbers of <br> size 256. No encryption. These are used for <br> comparison to the encrypted pairs. |

Table 3.5: Plaintext-ciphertext pairs generated for CAN analysis.
work well with the existing CAN setup, the images were made to be $256 \times 256$ pixel RGB images. This gave us 65536 pixel, each with 3 colors (red, green and blue), giving us a total of $256 \times 256 \times 3=196608$ values per image. We tried two methods of conversion:

- One bit per pixel. This gave us 65536 bits of plaintext/ciphertext per image, making it black and white. See Figure 3.8 for an example of one of these images.
- One bit per color per pixel. I.e. 3 bits per pixel. This gave us 196608 bits of plaintext/ciphertext per image file, making it a color image (RGB). See Figure 3.9 for an example of one of these images.

This gave us multiple plaintexts or ciphertexts per image, and the sets of images are therefore smaller than the sets of plaintexts and ciphertexts. Figure 3.10 shows how the system was set up, and Figure 3.5 shows an overview of the process.

Once we had a set of plaintext and ciphertext images, we could train the network on them.

As the Salsa20 algorithm consists of 80 quarter-rounds, we can expect the full algorithm to be more resistant to such analyses than a single quarterround function. And since the random pairs are not related, we use these as


Figure 3.6: Example of an incremented PT-CT pair.


Figure 3.7: Example of a random PT-CT pair.
a null hypothesis and a base result for our tests. If the CAN learns no better on Salsa20 pairs or quarter-round pairs than random pairs, we can conclude that this method does not seem viable. If, however, there is a difference, we can conclude that these functions are at least somewhat weak against a CANbased analysis. If, for some reason, the random sets have a significantly better learning rate than the other two sets, it may indicate that the PRF we use for generating the random pairs are weak against such analyses.


Figure 3.8: Example of a randomly generated PT-CT pair converted into RGB images.


Figure 3.9: Example of a randomly generated plaintext converted into an black and white image.


Figure 3.10: Illustration of our plaintext-based CAN analysis method.

## Encrypted images

In addition to creating pairs of texts, we took existing images, reshaped them in Matlab into the required sizes for our CAN. We also encrypted them using the Python Salsa20 implementation. See Figure 3.11 for an overview of this method.


Figure 3.11: Algorithm for CAN analysis on PT-CT pairs.
That way, we use the original images as PT and the encrypted ones as CT. For an example of a image generate from the CT, see Figure 3.12 The


Figure 3.12: Image version of the CT from an encrypted image of a face.
analysis is otherwise the same as last section: Train the network on the CTs, so it will hopefully be able to construct their respective PTs. This method is illustrated in Figure 3.13.


Figure 3.13: Illustration of our image-based CAN analysis.

## Chapter 4

## Results and discussion

### 4.1 Hamming distance

This section discusses the results from our differential analyses using the Hamming distance. First, we look at the results from Salsa20's quarter-round function, then we look at Salsa20's PRG function.

### 4.1.1 Quarter-round function

Salsa20 consists of 80 runs of the quarter-round function $(Q R)$, each of which progressively obfuscates the key more. If we define the $Q R$ function as:

$$
Q R(X) \rightarrow Y
$$

then our analysis as modifying $X$ into $X^{\prime}$ by changing some bits, and then measuring how the $Y$ reacts. If $Q R\left(X^{\prime}\right) \rightarrow Y^{\prime}$, and the $H D\left(X, X^{\prime}\right)=n$, what is $H D\left(Y, Y^{\prime}\right)=m$ ? As we progressively incremented $n$, we saw $m$ tend towards the expected equilibrium of half the length of $Y$. This analysis can be simplified to measuring:

$$
H D\left(Q R\left(X^{\prime}\right), Y\right)
$$

In Figure 4.1, the used values of $X$ are 1024 bits. This is done to show the trends more clearly. While the $Q R$ function is made for 128 bits, it can also be applied to other amounts of bits. The $x$ axis is in this case the amount of times the original $X$ has flipped a bit, i.e., $n$. The $y$ axis is the HD between the two values being measured, i.e., $m$. The lines in the legend are as follows:
0. $H D(X, Y)$

1. Convergence point of the Hamming distance between two random values.


Figure 4.1: Effects of flipping random bits in $X$.

## 2. $H D\left(Y, Y^{\prime}\right)$

## 3. $H D\left(X, X^{\prime}\right)$

Line 0 and 1 show that the $H D$ between an $X$ and its corresponding $Y$ is indistinguishable from the $H D$ between two random values. In other words, the Hamming distance is not showing any correlation between inputs and outputs of the $Q R$ function. Line 3 shows, unsurprisingly, that the Hamming distance between two words increase at about 1 bit per random bit flipped. Line 2 shows that the Hamming distance between two $Y$ values, where their corresponding $X$ values are $n$ bits distant from each other, drift towards the random/main sequence, or the expected value. It is however clearly distinguishable from random values, as long as $X$ and $X^{\prime}$ are relatively close. In other words, as the $H D\left(X, X^{\prime}\right)$ is sufficiently small, the $H D\left(Y, Y^{\prime}\right)$ is smaller than what one can expect from random. This indicates a lack of sufficient avalanche effect in the quarter-round function. Assuming

$$
H D\left(X, X^{\prime}\right)<\frac{\text { key size }}{8}
$$

$H D\left(X, X^{\prime}\right)$ should be easily distinguishable.


Figure 4.2: Averaging of effects on $Y$ when bits are flipped in $X$.

In Figure 4.2, we see 5 non-vertical lines. The vertical line is where the bits flipped needed for the Hamming distance to be within the range of expected random distances. In this case, about 11 bits. In the figure, the lines represent the following:
0. $H D\left(X^{\prime}, Y^{\prime}\right)$ as $n$ bits in $X^{\prime}$ are flipped.

1. $H D(X, Y)$ of random $X \mathrm{~s}$.
2. Minimum expected difference between two random $X$ s.
3. Maximum expected difference between two random $X \mathrm{~s}$.
4. Expected average difference between two random $X$ s.

### 4.1.2 Salsa20's PRG

We tried a similar analysis on Salsa20's PRG. In this case, we flipped random bits in the key, and saw how the output of the PRG reacted on the input. We can see the results in Figure 4.3. Line 1 shows how, unsurprisingly, how $H D\left(\mathrm{in}_{\text {original }}, \mathrm{in}_{\text {next }}\right)$ is roughly equal to 1 per flipped bits. Line 2 is the expected value for random inputs and outputs. This is also the expected value


Figure 4.3: Averaging of effects on the PRG output when bits are flipped in key.
for an encryption algorithm with sufficient confusion. This is where we would expect the $H D$ between random values to land. This is also where we would expect the $H D$ between a good encryption algorithm's input and output to land. And when we look at line 0 , this is indeed what we see. There seems to be no correlation or pattern between the amounts of bits flipped in the input $(n)$ and the $H D$ between the two values.

### 4.2 Context aggregation network

We made the CAN train on the 4 plaintext-ciphertext pairs, as well as the sets of graphical images. In Figure 4.4 we can see how the network trains on normal images, trending to 0 after a relatively short time.

For the random plaintext-ciphertext pairs, the network quickly stabilised the RSME and loss. However, it did not get close to 0 , and remained on a much to high error rate. We can see this in Figure 4.5 for the images encrypted by the quarter-round function, and in Figure 4.6 for encryption by Salsa20.

The results for the image based analysis gave show as that, while the images gave us different results, the network was not able to train towards a sufficiently low value for use in cryptanalysis and attacks. In Figure 4.7, we


Figure 4.4: Training trend for regular images.


Figure 4.5: Training trend for the $Q R$ text pairs.


Figure 4.6: Training trend for the Salsa20 text pairs.
can see that the network also plateaued far from 0 , when using regular patch sizes of $256 \times 256$. When using smaller patch sizes, we saw it still plateaued, but in a much more stable way. In Figure 4.8, we can see how the network trained on a $32 \times 32$ patch size. The result was similar when training overnight, about 300 epochs, 300000 iterations.


Figure 4.7: Training trend for the Salsa20 image pairs, with patch size of $256 \times 256$.


Figure 4.8: Training trend for the Salsa20 image pairs, with patch size of $32 \times 32$.

## Chapter 5

## Conclusion

This work attempted to answer the questions:

- Does Salsa20 seem to be secure against existing attacks?
- Can we break a weakened version of Salsa20?

Based on the found cryptanalysis research on Salsa20, there is little reason to think it is not sufficiently secure for normal use. There exists attacks more effective than brute-force, including side-channel attacks. Even so, these attacks are not practical, and so we conclude that Salsa20's security still holds up.

The analysis using the Hamming distance seem to show the quarter-round function does not have a sufficient avalanche effect to be an encryption algorithm by itself, but we also see that Salsa20 does not seem to suffer from the same effects. We therefore conclude that an attack based on this form of analysis, is not viable.

The analysis using the context aggregation networks shows little sign of effect. We therefore conclude that an attack using the CAN analysis we used, does not seem to have any feasibility.

### 5.1 Further work

While our context aggregation network did not show any signs of learning from the used data, it is possible that a modified loss function could work better. For example a loss function based on the Hamming distance.

As ChaCha and its quarter-round function is only slightly different, similar tests could be run at them to see if there is a significant difference.

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## Attachments

1. Implementation of Salsa and ChaCha, with analysis tools.
