Modeling N/S ratio and temperature influences on simultaneous biological denitrification and sulfide oxidation

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Abstract

A model describing the simultaneous removal of NO3⁻ and HS⁻ by microorganisms is presented here. The oxidation of HS⁻ (electron donor) can be controlled by the appropriate dosage of NO_3^- . The developed model, which includes variable process stoichiometry, attempts to predict the distribution of sulfur oxidation products. Stoichiometric coefficients are based on a 150 days experimental study of temperature (25-10 °C) and N/S ratio (0.35-1.30) effects. The model can be used as a prediction tool for autotrophic denitrification with HS⁻. Elemental sulfur production is included in the mathematical model, however, its accumulation and release (as SO₄²⁻) with increasing feed N/S ratio (e.g. leading to higher effluent than feed total sulfur mass at N/S = 1.30) is not simulated. A conceptual model to account for biological accumulation and release of elemental sulfur is proposed here.

Keywords: autotrophic denitrification, elemental sulfur production, mathematical modeling, sulfate production

1 Introduction

The presence of sulfide (H_2S) in wastewaters is an important issue concerning wastewater networks and treatment plants maintenance due to its corrosive properties (Ma et al., 2000). Low concentrations of H_2S (lower than 10 mg/L) are present in domestic wastewaters (Pikaar et al., 2011). The exposure to H_2S in gaseous form is toxic to human even at low concentrations and can paralyze the olfactory nerves and lead to death (Reiffenstein et al., 1992).

Biological wastewater treatment plants used to remove carbon, nitrogen and phosphorus can be inhibited by extensive presence of H_2S (Chen et al., 2008; Jin et al., 2013; Joye and Hollibaugh, 1995). It has been reported that anaerobic digestion process can be inhibited at concentrations from 50 mg H_2S/L (Chen et al., 2008). H_2S presence can vary due to the high complexity of the sulfur (S) cycle and its partial overlapping with cycles of other elements (i.e. C, Fe, Hg, N and Se). Knowledge of these cycles can be used for biochemical H_2S control and S removal.

Physicochemical H₂S removal is often used for H₂S removal (desulfurization) in industrial scale. The Claus

process, where elemental sulfur (S^0) is recovered from H₂S-containing gases under high temperature and oxygen (O_2) supply, is the most common method. Biological treatment, utilizing the unique properties of microorganisms, is gaining attention due to the environmental and economic advantages. Biological H₂S removal from wastewaters utilizes the ionic forms HS⁻ and/or S²⁻ (depending on pH) as the electron donor, while usually nitrate (NO₃⁻), nitrite (NO₂⁻) and O₂ are electron acceptor sources. The usage of these electron acceptors is not mutually exclusive, so they can be used together and separately. Addition of more than one electron acceptor can be applied to enhance the H₂S removal (Wang et al., 2015). Due to advantages such as a higher solubility of NO3⁻ than O2, NO3⁻ usage is studied here. It is argued that the continuous flow expanded granular sludge bed (EGSB) bioreactor is the most efficient design for biological desulfurization (Cai et al., 2010). Data from a previous EGSB study (Sposob et al., 2017a; 2017b) are used here.

The oxidation of HS⁻ can be controlled by the ratio between electron acceptor and electron donor to influence the relative amounts of the oxidation products: S^0 and sulfate (SO₄²⁻). Extensive experimental and theoretical studies on the appropriate conditions for simultaneous N and S removal, i.e. C/N/S ratio, pH, load and temperature, have been conducted (Di Capua et al., 2017; Guo et al., 2016; Huang et al., 2016; Mahmood et al., 2007; Montalvo et al., 2016; Reyes-Avila et al., 2004; Sposob et al., 2017a). Modeling can facilitate further understanding and optimization of simultaneous biological NO₃⁻ and HS⁻ removal. So far, a few models based on artificial neural networks (Wang et al., 2009) and kinetic approach (Wang et al., 2010; Xu et al., 2016, 2014) have been developed. The kinetic models are based on batch experiments where only the initial phase of the process is accounted for. Fixed stoichiometry based on assumed chemical reactions or based on calculated and/or experimentally obtained yield values also limits published models, since the ratio between electron acceptor and electron donor can completely alter the output (Cai et al., 2008; Sposob et al., 2017b). The models describing simultaneous removal of NO₃⁻ and HS⁻ should take into account the fact that effluents from this kind of treatment can contain several products especially at low N/S ratios. This is challenging since it has been observed in long-term experiment that $SO_4^{2^-}$ and S⁰ were produced at the same time at feed N/S ratio that theoretically should lead to S⁰ production only (Sposob et al., 2017a; Tan et al., 2016). It has also been observed that temperature has an impact on effluent sulfur components at constant N/S ratio (Sposob et al., 2017a). Thus, the need for the modeling including multicomponent effluent characteristic is required, especially in cases where lower N/S ratios are modeled.

The objective of this study is to develop a model for simultaneous removal of NO_3^- and HS^- at different N/S ratios and temperatures, which can be used to predict the distribution of produced sulfur components.

2 Methods and model development

2.1 Experimental design

The experimental trial was performed in a 0.5 L laboratory-scale EGSB reactor continuously fed by synthetic wastewater over 150 days. The feeding parameters are given in Table 1.

Table 1. Feeding parameters.

Time (d)	Temperature (°C)	N/S ratio	NO3 ⁻ (mM/L)	HS⁻ (mM/L)
1-25	25		1.08	
26-57	20	0.35		
58-90	15			
91-120				3.12
121-134	10	0.40	1.25	
135-142		0.60	1.87	
143-150		1.30	4.05	

Synthetic wastewater was supplied from two feed tanks (separate for electron acceptor and donor) to avoid contamination and possible reactions in feeding tank. In addition to electron acceptor and donor sources, vitamins, buffer, macro- and microelements were supplied as described in Sposob et al. (2017a), where the more detailed description of experiment is given.

2.2 Stoichiometry

The model is developed and evaluated based on the stoichiometry derived by Kleerebezem and Mendez, (2002) and data from continuous flow expanded granular sludge bed (EGSB) experiments (Sposob et al., 2017a; 2017b). The collected data consists information about concentrations of accumulated elemental sulfur (S_{acc}^{0}), nitrate (NO₃⁻), sulfate (SO₄²⁻), sulfide (HS⁻) and suspended elemental sulfur (S_{ss}^{0}) measured as thiosulfate (S₂O₃²⁻). Accumulated sulfur (S_{acc}^{0}) was calculated based on the difference between influent HS⁻ concentration and effluent concentrations of HS⁻, SO₄²⁻ and S_{ss}^{0} , according to Eq. 1 (Sposob et al., 2017a).

$$S^{0}_{acc} = HS^{-}_{inf} - HS^{-}_{eff} - SO_{4}^{2} - SO_{ss}$$
(1)

The basic chemical reactions (Eqs. 2, 3) and reactions combining both anabolism (biomass production) and catabolism (energy release) (Eqs. 4, 5) according to Kleerebezem and Mendez (2002) serve as the core for the model. However, these equations assume production of only one sulfur component at specific N/S ratio and does not include temperature impact.

 $\text{HS}^{-+1.6NO_3^{-}+0.6H^+} \rightarrow 0.8N_2 + \text{SO}_4^{2-}+0.8H_2O$ (2)

 $HS^{-}+0.4NO_{3}^{-}+1.4H^{+} \rightarrow 0.2N_{2}+S^{0}+1.2H_{2}O$ (3)

$$3HS^{+}3.9NO_{3}^{-}+0.2NH_{4}^{+}+HCO_{3}^{-}+1.7H^{+} \rightarrow$$

$$CH_{1.8}O_{0.5}N_{0.2}+1.95N_2+3SO_4^{2+2}-2.3H_2O$$

$$14.5HS^{-}+5NO_3^{-}+0.2NH_4^{+}+HCO_3^{-}+20.3H^{+} \rightarrow \qquad (2)$$

$$CH_{1.8}O_{0.5}N_{0.2}+2.5N_2+14.5S^0+17.4H_2O$$
(5)

The new stoichiometry applied here includes simultaneous NO_3^- and HS^- removal and possibility to produce two sulfur components: S^0 (without distinguishing the S^0 fractions) and SO_4^{2-} according to Eq. 6.

 $a\text{NO}_3^- + b\text{HS}^-\text{-}\text{S} \rightarrow c\text{S}^0 + d\text{SO}_4^{2-} + e\text{N}_2$ (6)

Where c and d depend on feed molar ratio between a and b (N/S ratio) and temperature (T) (Eqs. 7, 8).

$$c = f(N/S; T) \tag{7}$$

$$d = f(N/S; T)$$
(8)

2.3 Kinetics

Process kinetics is modeled based on the Monod equation for reaction rates and assuming one general microbial community of sulfide oxidizing bacteria (SOB). The growth of microorganisms is thus described using the Bailey's equation that includes both required substrates (Eq. 9). The biomass concentration is assumed constant in the simulations due to the conditions with high biomass content in the EGSB reactor and low biomass yield of autotrophic denitrification bacteria (Tchobanoglous et al., 2003), implying that reactor biomass changes are insignificant during the experiments used in this study. The growth parameters maximum growth rate (μ_{max}) and half-saturation constants (K_{HS-}, K_{NO3-}) applied are given in Table 2.

$$\mu = \mu_{max} \cdot X_{SOB} \left(\frac{S_{HS^-}}{K_{HS^-} + S_{HS^-}} \right) \left(\frac{S_{NO_3^-}}{K_{NO_3^-} + S_{NO_3^-}} \right)$$
(9)

Table 2. Growth	parameters.
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Parameter	Value	Source
μ_{max}	4.25 d ⁻¹	(Wang et al., 2010)
$K_{NO_3^-}$	7.84 mM NO ₃ -/L	(Xu et al.,
K _{HS} -	1.8 mM S ²⁻ /L	2016)

The mathematical model is implemented in the AQUASIM simulation software (Eawag, Switzerland). The established model is calibrated and used to simulate removal of NO_3^- and HS⁻. Simulation results are

compared with the obtained experimental data published in Sposob et al. (2017a, 2017b).

2.4 Temperature

Temperature has an impact on bacterial kinetic coefficients like μ_{max} and K_S leading to changes in the treatment efficiency. During the experimental trial the electron donor (HS⁻-S) removal changed from 98 (25 °C) to 89 % at 10 °C. Temperature also influenced the effluent composition of sulfur components in the experiment modeled here (Figure 1). Electron acceptor (NO₃⁻) removal was not significantly influenced by temperature as it was completely removed (effluent NO₃⁻ was detected only three times during 120 days temperature-trial).

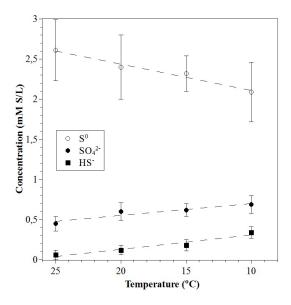


Figure 1. Average concentration of sulfur components at 25-10 $^{\circ}$ C and N/S = 0.35 (Sposob et al., 2017a).

With decreasing temperature and invariable feeding pattern, the share of S⁰ decreased while SO₄²⁻ together with HS⁻ increased. Performed free Gibbs energy calculations ($\Delta G^{0'}$) revealed that the reaction energy at the different temperatures remained nearly constant due to this shift in products formation from S^0 to SO_4^{2-} (Sposob et al., 2017a). The reaction energy maintained at invariable feeding conditions is dependent on the relationships given in Eqs. 10 and 11. The culture evidently preferred to use more NO₃⁻ per mole of HS⁻ at lower temperatures. Whether this is due to a shift in microbial community or a metabolic shift within cells is currently under investigation. Until such information is available empirical temperature an effect is implemented in the model by temperature dependent stoichiometric coefficients (Table 3) based on the experimental results given in Figure 1.

Reaction energy = oxidation to
$$S^0$$
 +
oxidation to SO_4^{2-} (10)

Reaction energy
$$\approx$$
 constant (11)

 Table 3. Temperature coefficient for stoichiometric

 parameters calculated based on the experimental trial.

Temperature	Tsulfur	Tsulfate
25	0.84	0.14
20	0.77	0.19
15	0.74	0.2
10	0.67	0.22

2.5 N/S ratio

Changes in N/S ratio have been reported as a way to control the level of HS⁻ oxidation (Cai et al., 2008). However, the results at different ratios at 10 °C show a significant offset from the theoretical values (Figure 2). The highest offset was obtained for S⁰. Experimental results equaled the theoretical values only at N/S = 1.30. A more detailed description of N/S ratio impact at psychrophilic conditions (10 °C) is given in Sposob et al. (2017b). Modeling effects of N/S ratios in Eq. 7 and 8 based on these observations is implemented through correction coefficients given in Table 4.

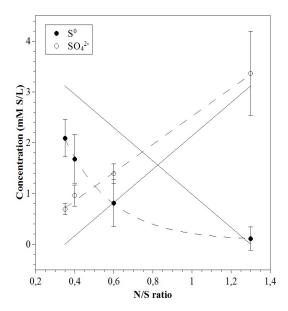


Figure 2. Average concentration of sulfur components at different N/S ratios at 10 °C. Whole lines are theoretical values based on Eqs. 4, 5 while dotted line connects the given experimental values.

 Table 4. N/S ratio coefficient for stoichiometric

 parameters calculated based on the experimental trial.

N/S ratio	N/S _{sulfur}	N/S _{sulfate}
0.35	1	1
0.40	0.81	1.41
0.60	0.48	2.05
1.30	0.06	4.36

3 Results and Discussion

Simulations, with the calculated coefficients (Table 3) of products distribution (S⁰ and SO₄²⁻) with different temperatures and constant feed N/S = 0.35 behaves similar to the experimental results (Figure 3). The implemented model with the temperature coefficients (Table 3) simulates the pseudo-steady state relative amounts of effluent S⁰ and SO₄²⁻. This may seem obvious since the coefficients are calculated based on average values for each temperature case of the same data set. The model, however, also simulates the transitions in relative amounts of products occurring following each 5 °C temperature drop (the initial part of each of the three last panels in Figure 3) quite The model significantly improved accurately. predictions at N/S = 0.35 compared to the equations (Eqs. 3, 5) that predict S^0 production only and no temperature effect.

Increasing the model complexity, including diversification of microbes and/or the implementation of energy terms, can further improve the model for better prediction of HS⁻ removal and products

distribution for a wider range of conditions. However, further experimental investigations are required to implement such.

Experimental data and predictions based on Kleerebezem and Mendez (2002) equations (Eqs. 4, 5) are compared in Figure 2 regarding N/S ratio effects on products distribution. The observed offset between experimental and theoretical values could be partly due to the oxidation of earlier accumulated S⁰ (reaction 3 in the schematic presentation of the studied process in Figure 4), but this is not explicitly included in the mathematical model. The reaction energy from HSoxidation is increasing with increased amount of NO3supplied. Probably both of these energy related phenomena influence the products distribution but insufficient results are yet available to distinguish these. Thus, further model refinement to include both hypothesized energy reactions separately is not attempted and the cumulative effect observed experimentally are covered by the coefficients given in Tables 3 and 4 and simulated (Figure 5).

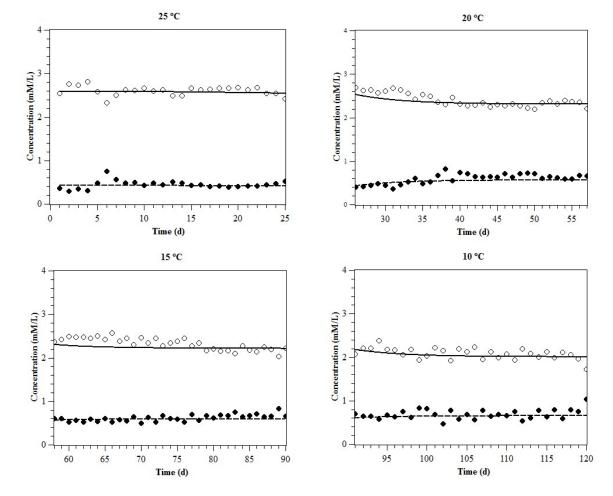


Figure 3. Model simulation results in comparison to experimental results at different temperatures. Solid and dash line represent simulated results for S⁰ and SO₄²⁻, respectively. Scatter points represent experimental results for S⁰ (\circ) and SO₄²⁻ (\bullet).

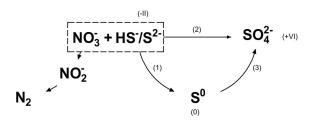


Figure 4. The scheme of autotrophic denitrification with HS⁻ as electron donor.

The simulations with the applied coefficients related to N/S ratio (Table 4) significantly improved predictions compared to those in Figure 2, except for N/S = 1.30, where simple stoichiometric calculations matched the experimental values best. The poor simulation of experimental results at N/S = 1.30 is assumed to be due to the fact that reaction 3 in Figure 4 is not explicitly accounted for in the model and that this reaction is especially important at this stage. This is due to the experimental scenario which at the beginning was focused on S⁰ production leading to its accumulation, as energy storage for the microorganisms. This S⁰ energy reserve in the reactor was oxidized to SO_4^{2-} and is especially visible at N/S = 1.30. This implies that a more refined future model of simultaneous biological removal of HS⁻ and NO₃⁻ needs to consider the effect of S⁰ accumulation and its possible oxidation (Figure 4) as occurred here under N/S ratio effects trial.

The energy related aspects discussed here are not included in the previously published models since these are based mainly on batch experiments and high N/S ratio situations. The observed phenomena probably occur only in cases when the N/S ratio is in or close to the range investigated here and are most observable when increasing from low (S⁰ production related) to high N/S ratios (SO42- production related). It can therefore be useful to develop the model further to better account for accumulation and consumption of S⁰. Some relevant information is available, such as: kinetics for S⁰ leaching and usage as electron donor is available (Franzmann et al., 2005; Gourdon and Funtowicz, 1998; Koenig and Liu, 2001). Models including similar accumulation phenomena related to energy storage are developed, i.e. ASM2d where the accumulation and

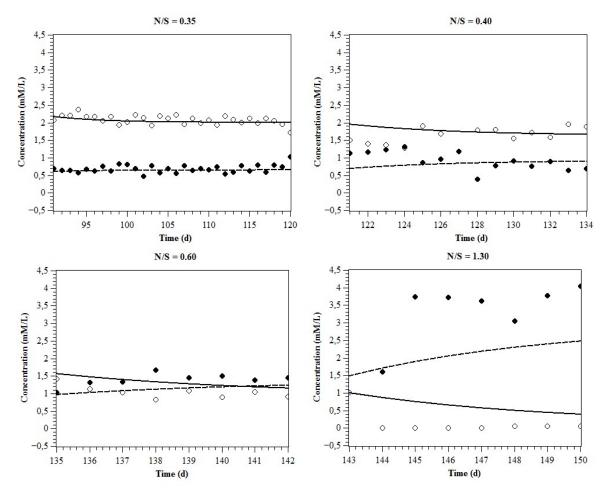


Figure 5. Model simulation results in comparison to experimental results at different N/S ratios at 10 °C. Solid and dash line represent simulated results for S⁰ and SO₄²⁻ respectively. Scatter points represent experimental results for S⁰ ($^{\circ}$) and SO₄²⁻($^{\circ}$).

consumption of polyhydroxybutyrate (PHB) and polyphosphate (PP) are taken into account (Henze et al., 1999). However, the factors triggering the oxidation of accumulated S⁰ are not clear. It has been reported that the oxidation can only occur when the source of reduced sulfur compounds is depleted (Schedel and Trüper, 1980), but oxidation of accumulated S⁰ can obviously occur (e.g. Figure 2) and be influenced by both temperature and N/S ratio changes when HS⁻ (sulfur reduced compound) is available (Sposob et al., 2017b, 2016). The observation that S⁰ leaching increases with temperature (Franzmann et al., 2005) should also be accounted for in the further model development.

4 Conclusions

The presented model can serve as a prediction tool for autotrophic denitrification with HS⁻ as supplied electron donor, to account for effects of temperature and feed N/S ratio.

The model was able to simulate sulfur compound products distribution at different temperatures, more accurately at low than higher N/S ratios (N/S range 0.35 to 1.30).

The phenomena of S^0 production included in the mathematical model does not take into account its accumulation and release (as SO_4^{2-}). Thus, adequate prediction of products distribution caused by N/S ratio step increases (leading to higher concentration of sulfur components in the effluent than fed into the reactor) was not obtained. Therefore, a conceptual model is proposed to account for biological accumulation and release of S^0 . Further investigations on N/S ratio effects on S^0 accumulation and release can yield a more refined model of simultaneous biological removal of HS⁻ and NO₃⁻.

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